
Python Control Systems Toolbox

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The *control-toolbox* is a Python Library for implementing and simulating various systems and control strategies.

Current Supported Functionality:

- System modeling with Transfer Functions and State Space Representations.
- Time Domain Response.
- Frequency Response.
- System Representation conversion: State Space model to Transfer Function and vice versa.
- Block diagram algebra: Series and Parallel.
- Stability Analysis.
- Root Locus.
- Bode Plot.
- Parameterization of System.
- Pole-Zero / Eigenvalue plot of systems.
- Feedback analysis.
- PID control.
- Observability and Controllability.
- Full State Feedback
- Full State Observer
- Linear Quadratic Regulator(LQR)
- Linear Quadratic Estimator(LQE) / Kalman Filter
- Linearization.
- System Identification.

Future Updates:

- Linear Quadratic Gaussian Control.
- Extended Kalman Filter.
- Unscented Kalman filter.
- Model Predictive Control.

Documentation:

The *control-toolbox* is a Python Library for implementing and simulating various systems and control strategies. All information regarding this library can be found here, including the documentation and usage of the modules.

1.1 Installation

The *control-toolbox* library can be installed using pip.

To install it use:

```
pip install control-toolbox
```

1.2 Development

To get the latest unreleased version

```
git clone https://github.com/rushad7/control-toolbox.git
```

1.3 Getting Started

To start using the package, we simply import it as:

```
>>> import control
```

System Representation

Systems can be defined by Transfer Functions and State Space models. Both system representations provide near identical utility.

2.1 Transfer Functions

A Transfer Function is the Laplace Transform of the ratio of output to input, and are mathematically described as:



To define a system in terms of a Transfer Function, use the *TransferFunction* class.

```
>>> import control
>>> s = control.TransferFunction(num, den)
```

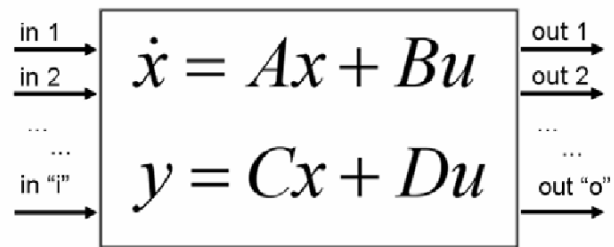
Here *num* and *den* can be lists or numpy arrays

2.2 State Space Models

Space State models are mathamatically described as:

To define a system as Space State model, use the *StateSpace* class.

```
>>> import control
>>> s = control.StateSpce(A,B,C,D)
```



Here, A,B,C,D are ndarrays.

Note: A system can be defined by any of the two representations above. If a particular method is needed but is not provided for the given system representation (which is unlikely), you can convert the system model to the desired representation using the *convert2TF()* or *convert2SS()* method.

Function Reference

The following table lists the classes and methods that can be used to model and simulate various systems and control strategies.

3.1 System Definition

Class	Description
<i>TransferFunction(num, den)</i>	Creates a Transfer Function system object
<i>StateSpace(A,B,C,D)</i>	Creates a State Space system object

3.2 Transfer Function Methods

Method	Description
<i>display()</i>	Displays the Transfer Function system
<i>parameters(settling_time_tolerance=0.02)</i>	Returns the parameters of the system
<i>response(input_type, time_period=10, sample_time=0.05, ret=False, show=True)</i>	Returns the time domain response on the system
<i>pzplot(ret=True)</i>	Plots the Pole-Zero plot of the system and return poles and zeros
<i>stability()</i>	Returns the stability of the system
<i>rootlocus(tf, gain_range=10.0)</i>	Returns Root Locus of the system

3.3 State Space Methods

Method	Description
<i>display()</i>	Displays the State Space system
<i>convert2TF()</i>	Converts State Space model to Transfer Function
<i>contr()</i>	Controllability of the system
<i>obs()</i>	Observability of the system
<i>stability()</i>	Stability of the system
<i>eigplot(ret=True)</i>	Plots eigenvalues/poles of system
<i>StateResponse(t, initial_cond, u, ret=False, show=True)</i>	Returns and plots state response
<i>OutputResponse(t, initial_cond, u, ret=False, show=True)</i>	Returns and plots output response

3.4 System Connections

Method	Description
<i>feedback(G, H=1.0, feedback_type="negative")</i>	Creates a Feedback Object
<i>reduce.series(tf1, *tfn)</i>	Return the series connection (tfn * ...
<i>reduce.parallel(tf1, *tfn)</i>	Return the parallel connection (tfn + ...

3.5 Frequency Domain Analysis

Method	Description
<i>bode.freqresp(tf)</i>	Returns the Frequency Response of the system
<i>bode.bode(tf)</i>	Returns the Bode Plot of the system

3.6 PID Controller Design

Method	Description
<i>PID(Kp, Ki, Kd, tf)</i>	Creates a PID object
<i>response(input_type, time_period=10, sample_time=0.05, ret=False, show=True)</i>	Return the response of the system after PID control
<i>tune(input_type="step", set_point=1, num_itr=70, rate=0.00000000001, lambd=0.7)</i>	Tune the PID coefficients
<i>display()</i>	Display the PID block
<i>reduced_tf</i>	Displays the reduced Transfer Function (Controller + Plant)

3.7 State Feedback Design

Method	Description
<i>StateFeedback(ss)</i>	Creates a StateFeedback object
<i>solve(roots)</i>	Calculates the State Feedback gain matrix
<i>model(k_ref=1)</i>	Retruns StateSpace object after applying State Feed-back

3.8 State Observer Design

Method	Description
<i>StateObserver(ss)</i>	Creates StateObserver object
<i>solve(roots)</i>	Calculates the State Observer gain matrix
<i>model(k_ref=1)</i>	Retruns the StateSpace object after applying State Observation

3.9 Linear Quadratic Regulator(LQR)

Method	Description
<i>LQR(ss, Q, R, N)</i>	Creates an LQR object
<i>solve()</i>	Calculates the optimal gain matrix
<i>model()</i>	Returns the StateSpace object after applying State Observation

3.10 Kalman Filter / Linear Quadratic Estimator(LQE)

Method	Description
<i>KalmanFilter(ss, Q, R, P=None, x0=None)</i>	Creates a KalmanFilter object
<i>predict(u = 0):</i>	Predict next state
<i>update(z):</i>	Update Predictions
<i>solve(measurements, ret_k=False, ret_x=False):</i>	Returns the Predictions, Kalman Gain, and States of the system

3.11 Linearization

Method	Description
<i>linearize(ss, x0, x_op, u_op, y_op)</i>	Creates a <i>linearize</i> object
<i>linearize()</i>	Linearizes the system and returns the systems state space matrices

3.12 System Identification

Method	Description
<i>SystemIdentification</i> (<i>path_x</i> , <i>path_x_dot</i> , <i>path_y</i>)	Creates a <i>SystemIdentification</i> object
<i>fit</i> (<i>num_epochs</i> =500):	Models the system
<i>model</i> ():	Returns the dictionary of system matrices

- `genindex`